



MINISTÉRIO DA CIÊNCIA E TECNOLOGIA  
INSTITUTO NACIONAL DE PESQUISAS ESPACIAIS

INTERNATIONAL SYMPOSIUM AND  
WORKSHOP ON ASTROCHEMISTRY

Understanding extraterrestrial molecular complexity  
through experiments and observations



# Theoretical Studies of $HS+HX=H_2S+X$ , with $X = H, F, Cl, Br$ and $I$

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LAP/INPE - MCTIC

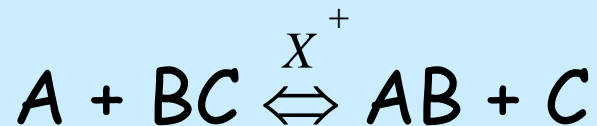
03-08/07/2016

# *Summary*

- Outline of theory
- Results
- APUAMA (p.69)
- Conclusion

# Transition State Theory

➤ For a bimolecular reaction:



➤ The thermal reaction rate is given by:

$$k_{TST} = \frac{k_B T}{h} \frac{Q_{X^+}}{Q_A Q_{BC}} \exp\left(-\frac{V_a^{G^+}}{RT}\right)$$

➤ and the barrier is:

$$V_a^{G^+} = V^+ + \varepsilon_{ZPE}$$

# Partition Function

$$Q = Q_{trans} Q_{rot} Q_{vib} Q_{elet}$$

	Degrees of freedom	Partition Function	Magnetude order
Translation	3	$Q_{trans} = \left( \frac{2\pi m k_B T}{h^2} \right)^{3/2}$	$10^{33} \text{ m}^3$
Rotation - 2D	2	$Q_{rot-2D} = \left( \frac{8\pi^2 I k_B T}{\sigma_e h^2} \right)$	$10 - 10^2$
Rotation - 3D	3	$Q_{rot-3D} = \left[ \frac{\sqrt{\pi}}{\sigma_e} \left( \frac{8\pi^2 I_m k_B T}{h^2} \right)^{3/2} \right]$	$10^2 - 10^3$
Vibration	$n = 3N - 5$ $n = 3N - 6$	$Q_{vib} = \prod_{i=1}^n \left[ 1 - \exp\left( -\frac{h c \nu_i}{k_B T} \right) \right]^{-g_i}$	$1 - 10^n$
Electronic	-	$Q_{elet} = \sum_{i=0}^n g_i \exp\left( -\frac{\epsilon_i}{k_B T} \right)$	1

➤ Zero point energies:

$$\varepsilon_{ZPE} = \frac{1}{2} \sum_i h d_i \omega_i$$

➤ Tunneling correction:

$$k_{TST}^Z(T) = \kappa(T) k_{TST}(T)$$

➤ Skew angle:

$$\beta = \arccos \left[ \frac{m_A m_C}{(m_A + m_B)(m_B + m_C)} \right]^{1/2}$$

➤ Arrhenius Form:

$$k = AT^n \exp\left(-\frac{E_a}{RT}\right)$$

➤ Wigner transmission coefficient:

$$\kappa(T) = 1 + \frac{1}{24} \left| \frac{h\omega^+}{k_B T} \right|^2$$

➤ Eckart transmission coefficient:

$$\kappa(T) = \frac{\exp(\Delta V^\ddagger / RT)}{RT} \int_0^\infty \exp(-E/RT) \Gamma(E) dE$$

➤ Small Curvature transmission coefficient:

$$\kappa(T) = \frac{\int_0^\infty P(E) \exp(-E/k_B T) dE}{\int_{V_a^G}^\infty P(E) \exp(-E/k_B T) dE}$$

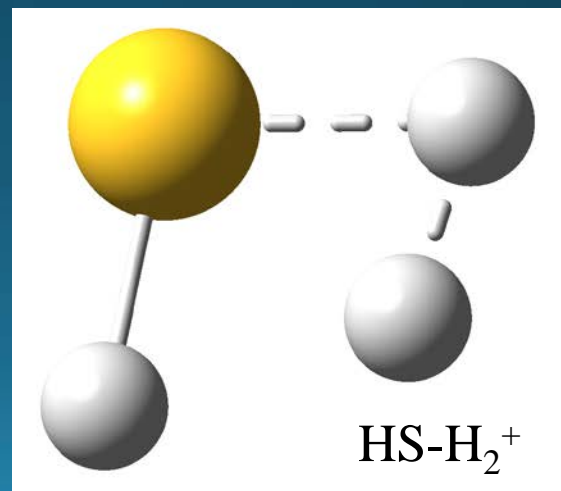
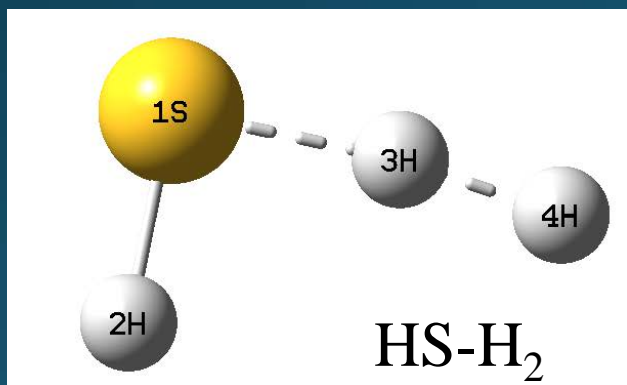
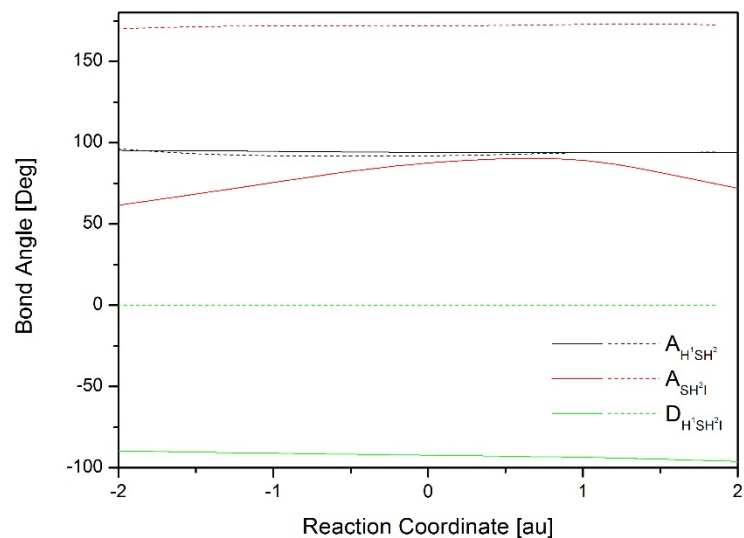
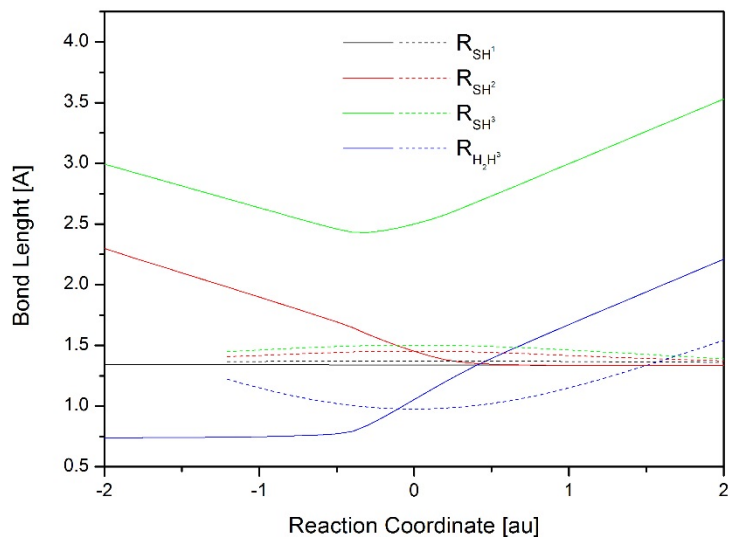
# *Results – HS+HS=H<sub>2</sub>S+X*

- Gaussian09
- Geometries and frequencies at MP2/aug-cc-pVTZ, iodine with DGZVP
- Energies at CCSD(T)/aug-cc-pVQZ
- IRC
- APUAMA (p. 69)
- Reactants and Products  $\Rightarrow D_e, \Delta H_f, S, C_p, H, \alpha$

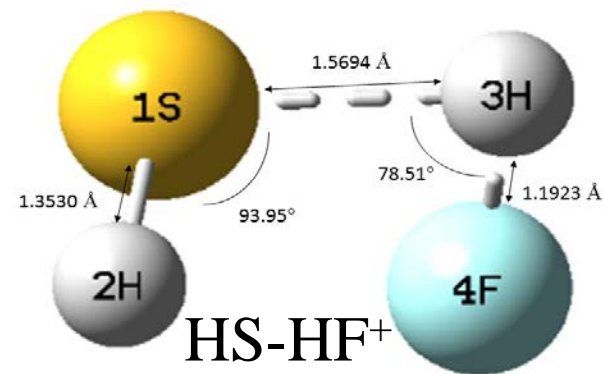
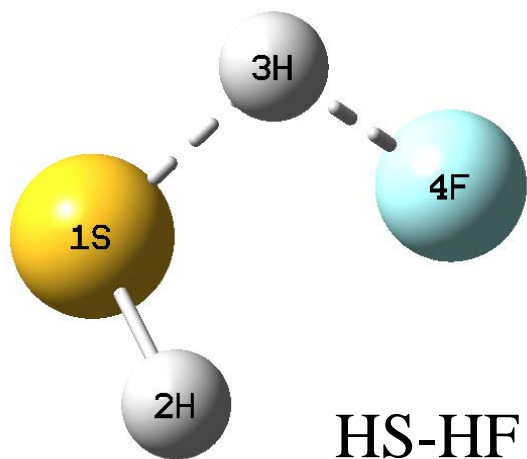
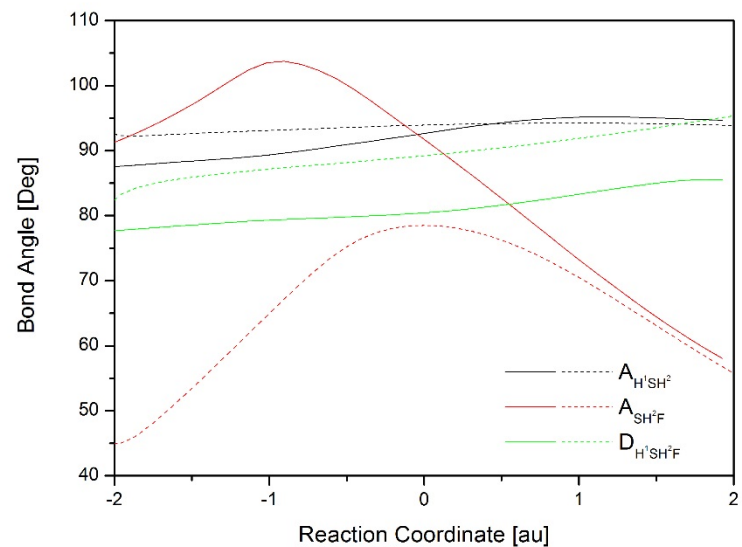
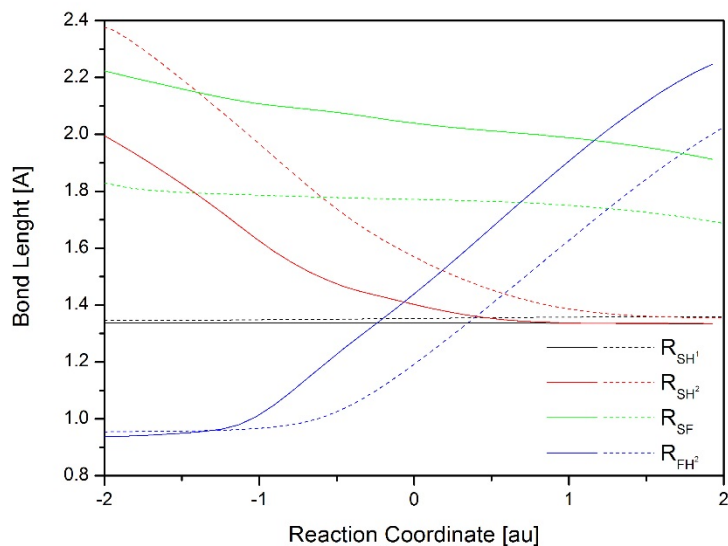
	R [ $\text{\AA}$ ]	A [Deg]
HS	1.3466	
HS <sup>+</sup>	1.3670	
H <sub>2</sub>	0.7431	
HF	0.9210	
HCl	1.2787	
HBr	1.4133	
HI	1.5969	
H <sub>2</sub> S	1.3419	92.31
H <sub>2</sub> S <sup>+</sup>	1.3614	93.08
H <sub>3</sub> S <sup>+</sup>	1.3537	94.33

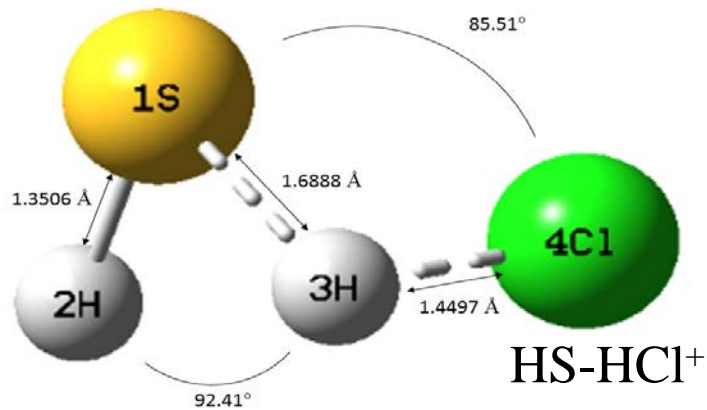
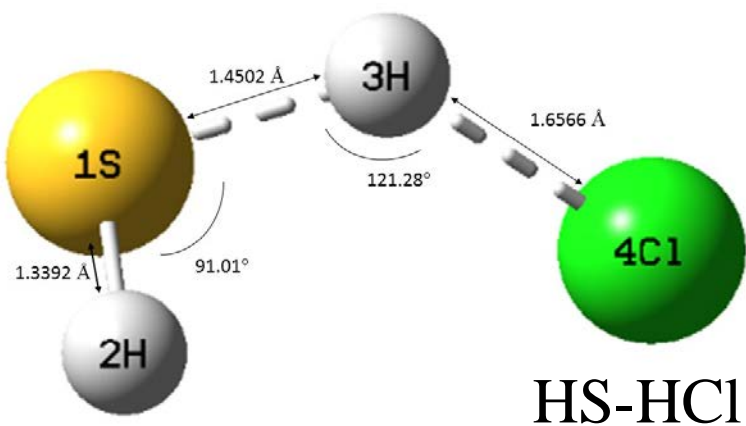
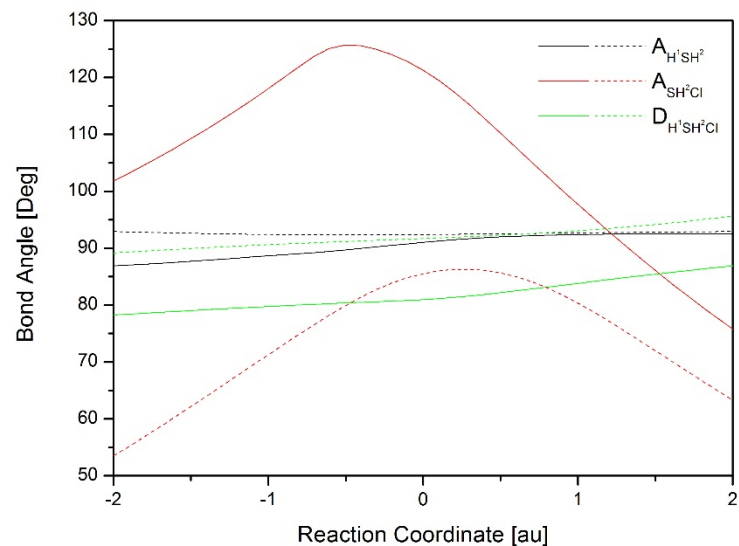
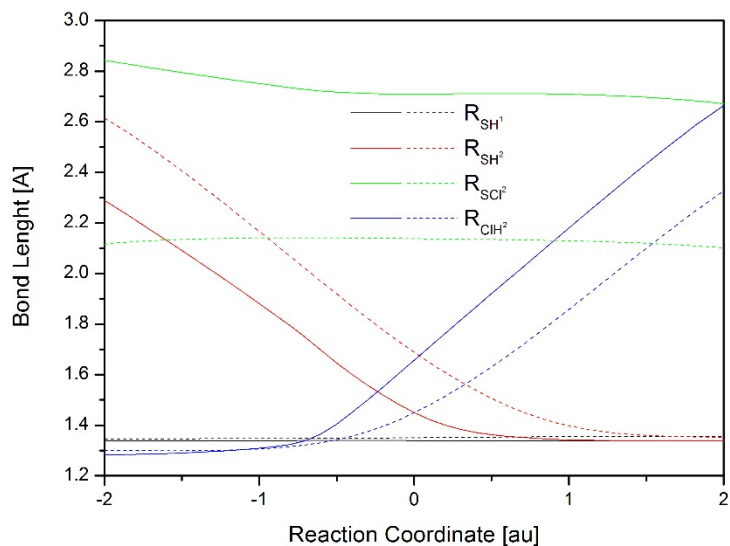


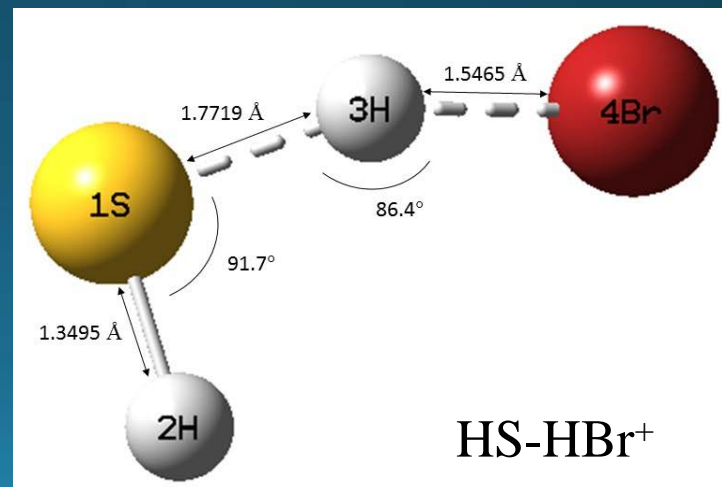
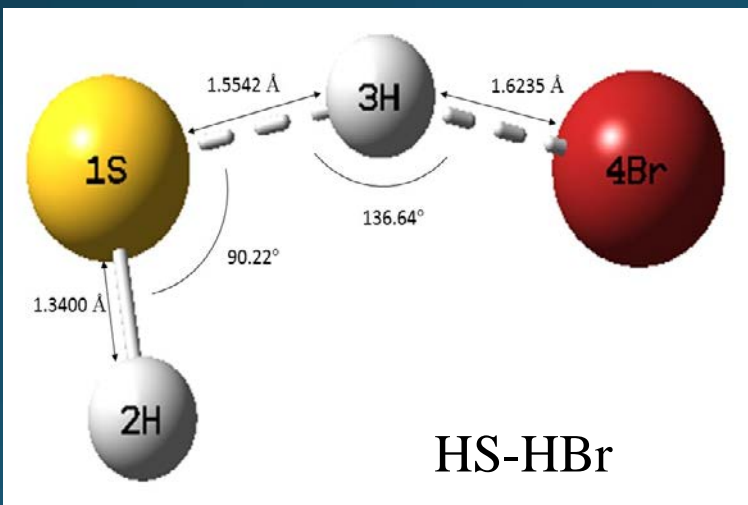
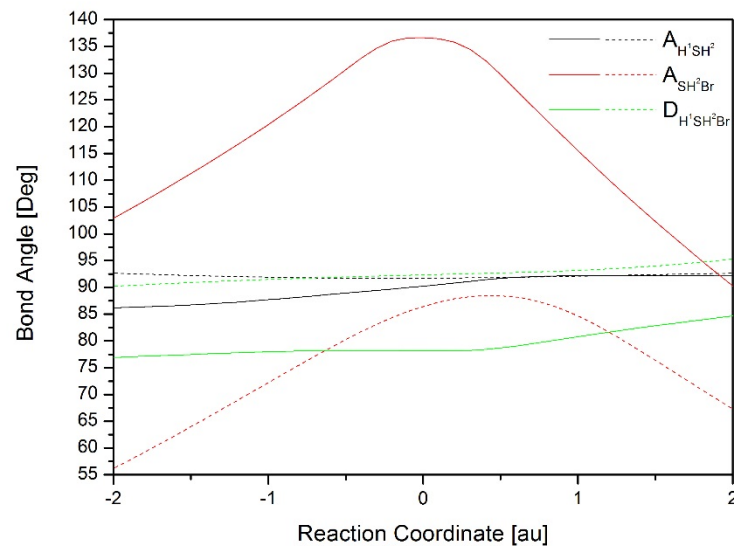
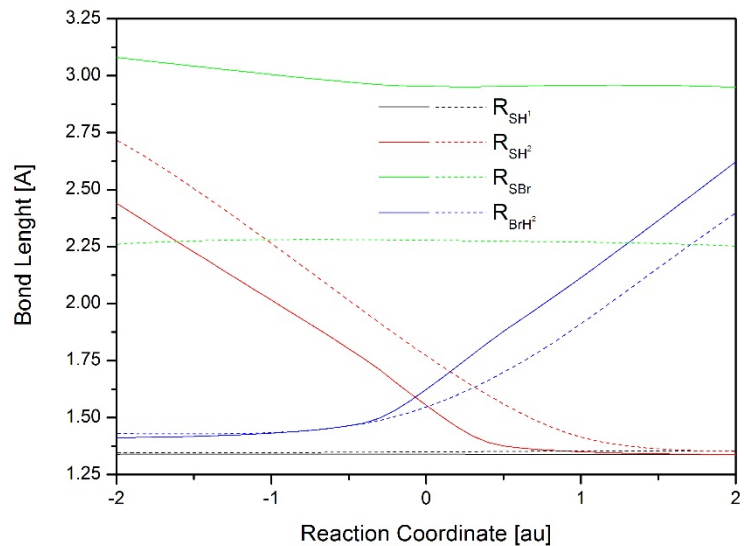
	$\omega_1$	$\omega_2$	$\omega_3$	$\omega_4$	$\omega_5$	$\omega_6$
H <sub>2</sub>	4400.44					
HBr	2696.15					
HCl	2992.74					
HF	4125.47					
HI	2391.05					
HS	2685.91					
HS <sup>+</sup>	2568.28					
H <sub>2</sub> S	1206.28	2710.87	2727.33			
H <sub>2</sub> S <sup>+</sup>	1185.75	2590.71	2597.93			
H <sub>3</sub> S <sup>+</sup>	1058.31	1222.50	1222.83	2626.53	2634.38	2634.39
HS-H <sub>2</sub>	-1695.19	481.74	533.72	1115.00	1401.81	2767.15
HS-HF	-1151.89	570.48	1064.48	1206.95	2414.77	2774.52
HS-HCl	-1129.49	243.98	460.96	1033.34	1667.44	2764.15
HS-HBr	-1344.79	191.56	428.55	880.58	1099.35	2757.32
HS-HI	-1321.67	158.90	257.39	413.00	751.55	2744.59
HS-H <sub>2</sub> <sup>+</sup>	-1323.64	829.24	1354.59	2003.99	2381.60	2569.03
HS-HF <sup>+</sup>	-1651.22	669.41	867.75	945.73	2080.57	2665.18
HS-HCl <sup>+</sup>	-1215.39	497.89	699.06	903.15	1929.47	2677.56
HS-HBr <sup>+</sup>	-1106.53	407.14	617.33	863.70	1908.39	2685.26
HS-HI <sup>+</sup>	-1190.34	336.65	585.12	810.35	1647.87	2711.26



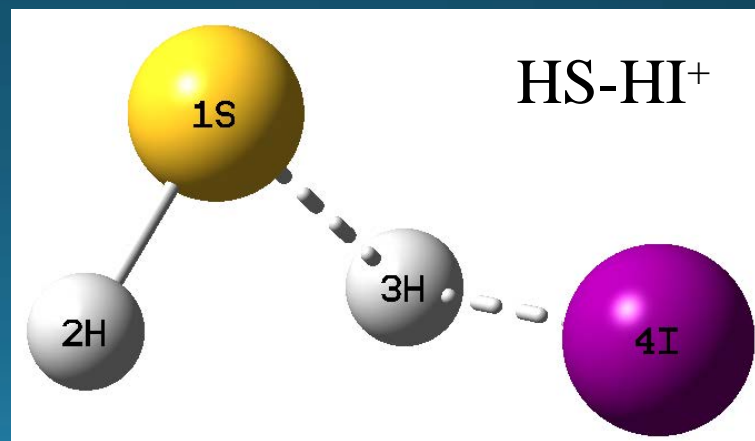
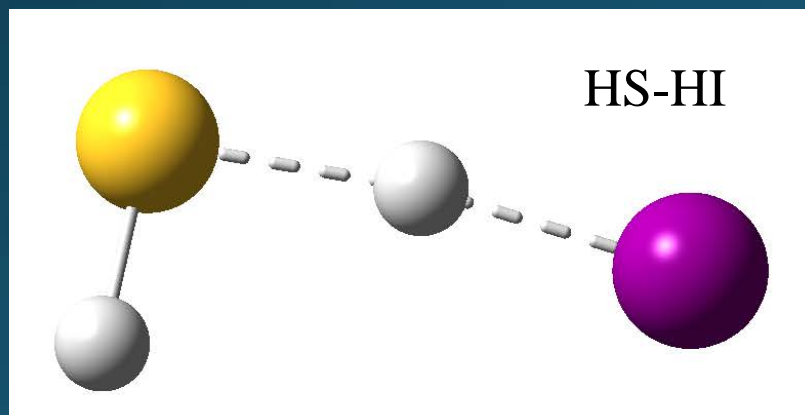
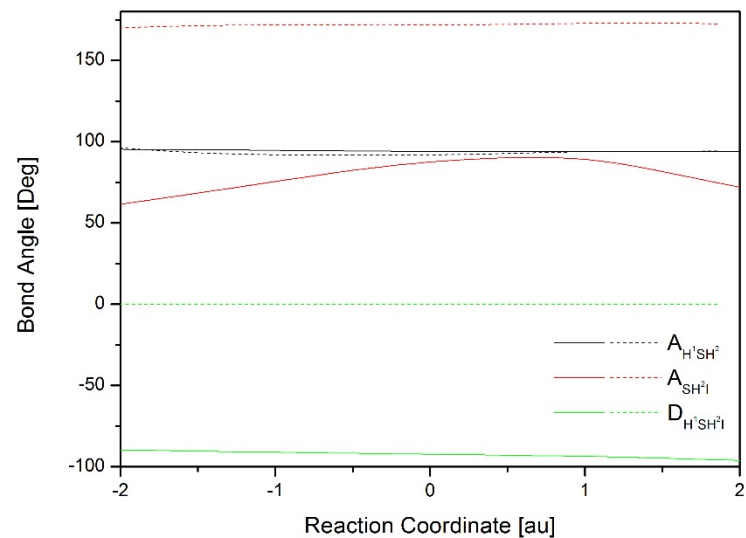
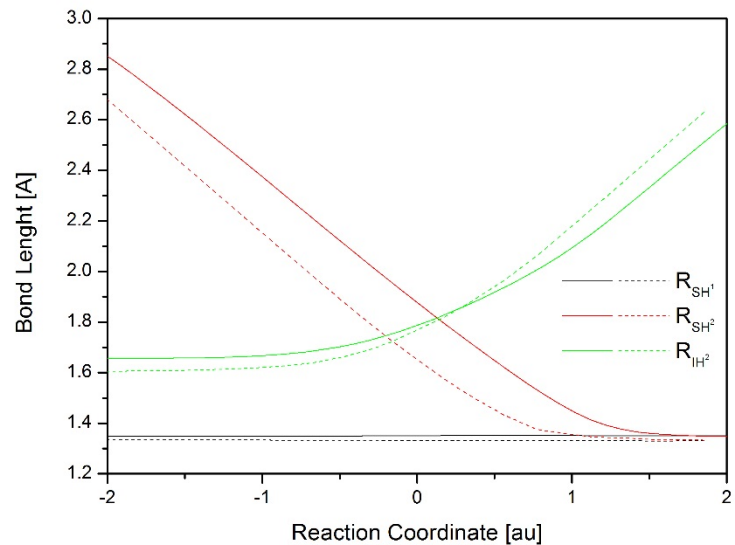
# $HS+HF=H_2S+F$ or $HS^++H_2=H_2S^++F$







# $HS+HI=H_2S+I$ or $HS^++HI=H_2S^++I$



APUAMA

Input Type

**Reactants** **TS** **Products** **Reaction** **Rovibrational Levels**

Entry Entry Entry Entry Entry

Check

Check input

Calculate

# APUAMA

a software tool for reaction rate calculations

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2015

## A simple program to determine the reaction rate and thermodynamic properties of reacting system

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### Abstract

We developed a simple program to determine the reaction rate by using conventional transition state theory with the Wigner transmission coefficient and also the thermodynamic properties of the species. The hydrogen abstraction in the reaction  $\text{NH}_3 + \text{H} \rightarrow \text{NH}_2 + \text{H}_2$  is used as a model to demonstrate the program usage. The rate constants have been computed for the gas-phase chemical reaction over the temperature range of 200–4000 K. Our data are in a good agreement with the published data for this reaction.

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*Keywords:* Kinetics; Thermal rate constants; Conventional transition state theory; Direct dynamics; Bimolecular abstraction; GAUSSIAN 98; Thermodynamic properties

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# Theoretical Study of the Reactions $\text{BF}_3 + \text{BX}$ , Where $X = \text{H}$ or $\text{N}$

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**ABSTRACT:** This work presents the rate constant for the gas-phase reaction  $\text{BF}_3 + \text{BX}$ , where  $X = \text{H}$  or  $\text{N}$ , over the temperature range of 200–4,000 K. Conventional transition state theory (TST) is used to study these reactions. Geometries, frequencies, and the potential energy for reactant, products, and saddle point are obtained from accurate electronic structure calculations performed with the GAUSSIAN 98 program. The reaction rate for these reactions are determined using a simple code developed for this task. © 2005 Wiley Periodicals, Inc. *Int J Quantum Chem* 103: 685–694, 2005

Input Type

**Reactants**    **TS**    **Products**    **Reaction**    **Rovibrational Levels**

Entry    Entry    Entry    Entry    Entry

Check

Check input

Calculate

Clear

EXAMPLE FOR REACTANTS, TS AND PRODUCTS (Input is only red text) (Unity in green)

Name of Specie	# Atoms	# Freq	Type (1 for atom, 2 for linear and 3 for non linear)	Sigma (external simetry)
<b>C2O2</b>	<b>4</b>	<b>5</b>	<b>3</b>	<b>1</b>

Mass (atomic unity)	Coordinates (A) x	y	z
<b>12.00000</b>	<b>-0.0575219378</b>	<b>0.0646325147</b>	<b>0.0601924965</b>
<b>12.00000</b>	<b>0.0785799255</b>	<b>-0.0718357288</b>	<b>2.7006328027</b>
<b>15.99491</b>	<b>0.3417312904</b>	<b>-0.0693771228</b>	<b>1.528709391</b>
<b>15.99491</b>	<b>0.0237332029</b>	<b>0.1775441321</b>	<b>3.8456409101</b>

Energy (Hartree)	Negative Frequency (only for TS, leave blank for reactants and products) (cm <sup>-1</sup> )
<b>-225.9941208</b>	<b>-907.7706</b>

Frequencies (cm<sup>-1</sup>)

**92.6917**  
**431.6611**  
**534.1647**  
**1067.5773**  
**2239.6699**

A = Angstrom

EXAMPLE FOR REACTION

Name of Reactant 1	Name of Reactant 2	Name of Product 1	Name of Product 2
<b>CO</b>	<b>CO</b>	<b>C</b>	<b>CO2</b>

Energy of reactants or RC (Hartree)	Energy of products or PC (Hartree)
<b>-226.2848222</b>	<b>-226.0812013</b>

Input Type

**Reactants**    **TS**    **Products**    **Reaction**    **Rovibrational Levels**

Entry    Entry    Entry    Entry    Entry

Check

Check input

Calculate

Clear

# Atoms	# Freq	CO Type	Sigma	Energy	+	# Atoms	# Freq	CO Type	Sigma	Energy
2	1	linear	1	-113.190		2	1	linear	1	-113.190

OCOC									
-->	# Atoms	# Freq	Type	Sigma	Energy	-Freq	-->		
	4	5	non linear	1	-226.075	-1485.742			

# Atoms	# Freq	C Type	Sigma	Energy	+	# Atoms	# Freq	CO2 Type	Sigma	Energy
1	0	atom	1	-37.736		3	4	linear	2	-188.390

Reactant 1	Reactant 2	Product 1	Product 2	EnergyRC	EnergyPC
CO	CO	C	CO2	-226.176	-226.381

Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

Check

Check input

Calculate

Clear

**Successfully calculated rate, choose the outputs below.**

For rate and correction of tunneling.

Rate

For minimum energy path (MEP).

MEP

For energy barriers, and enthalpy.

Barriers

For rate as Arrhenius.

Arrhenius

**all data is saved in**

C:/Research/APUAMA/COCO/OCOC\_Outputs/

Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

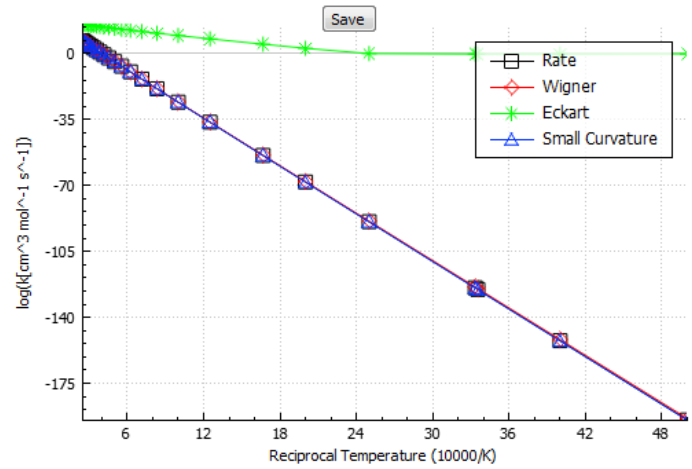
Check

Check input

Calculate

Back

The rate was calculated with tunneling corrections Wigner, Eckart, and small curvature. The following graph compares these rates with the reciprocal temperature.



the data were saved as 'kt.dat'.

Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

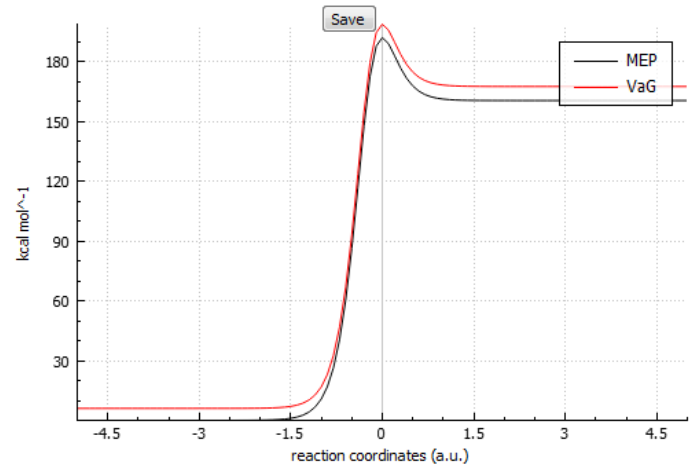
Check

Check input

Calculate

Back

The following graph compares the MEP and zero point energy correction with the reaction coordinates.



the data were saved as 'MEP.dat'.

Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

Check

Check input

Calculate

**Enter with rotational and vibrational level (v,J)  
(between 0 and 49) for the species you want.**

	Reactant 1	Reactant 2	Product 1	Product 2
	<b>CO</b>	<b>CO</b>	<b>C</b>	<b>CO2</b>
v	7	8	0	0
J	10	5	0	0

the data were saved as "EspecieName\_En.dat".

Enter

Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

Check

Check input

Calculate

Back

$$V_a^G f = 98.5943 \quad \text{kcal mol}^{-1}$$

$$V_a^G r = 31.2769 \quad \text{kcal mol}^{-1}$$

$$DH f = 67.1356 \quad \text{kcal mol}^{-1}$$

$$\text{Beta} = 58.5138 \quad \text{DEG}$$

the data were saved as 'ke.dat'.



Input Type

**Reactants**

Entry

**TS**

Entry

**Products**

Entry

**Reaction**

Entry

**Rovibrational Levels**

Entry

Check

Check input

Calculate

Back

$$k(T) = AT^n \exp(-E_a/RT)$$

	A	n	Ea
k(t)	9.539106e+09	2.021353e+00	9.710728e+04
Wigner	3.164477e+09	2.142473e+00	9.620251e+04
Eckart	1.526443e-18	9.548460e+00	7.532965e+03
CVT	9.219141e+09	2.022117e+00	9.723812e+04

the data were saved as 'Arrh.dat'.

 OCOC\_(07,05)\_(08,02)\_Outputs

 OCOC\_(07,10)\_(08,05)\_Outputs


 OCOC\_(08,02)\_(10,05)\_Outputs


 OCOC\_(09,07)\_(10,05)\_Outputs

 OCOC\_(10,10)\_(10,10)\_Outputs

 OCOC\_Outputs

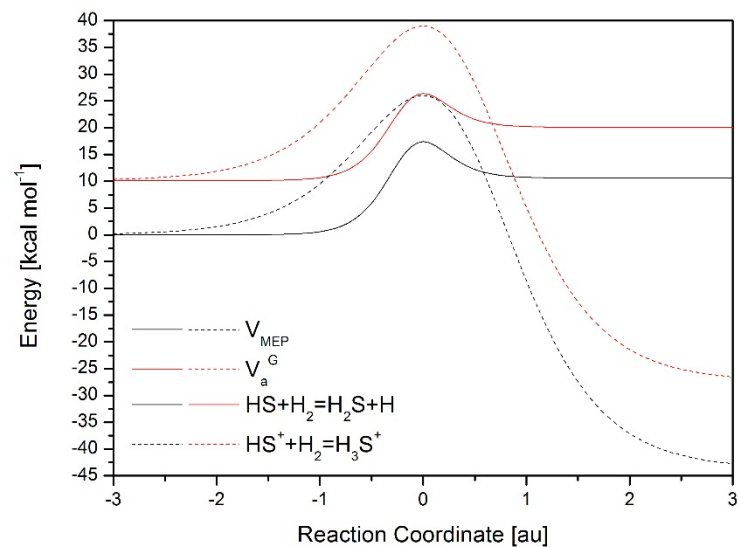
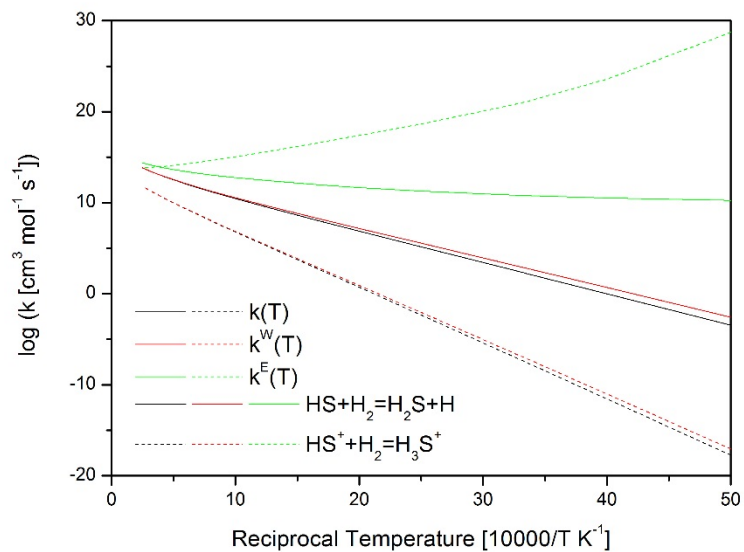
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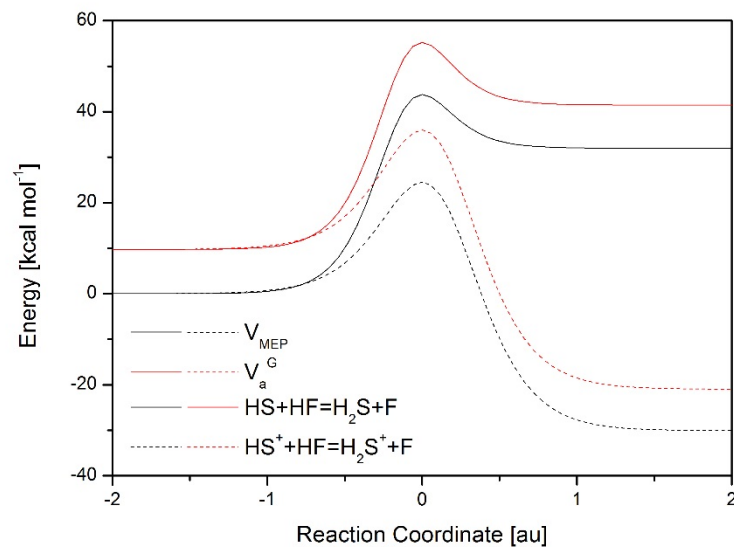
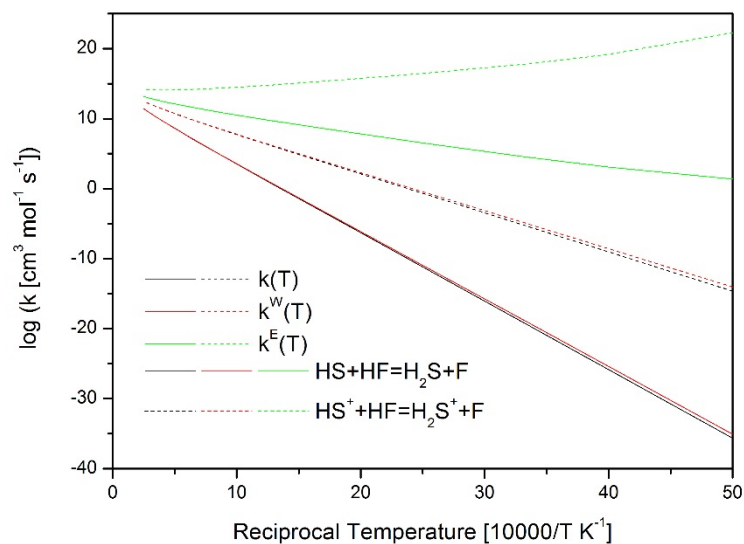
 produtos.dat

 reacao.dat

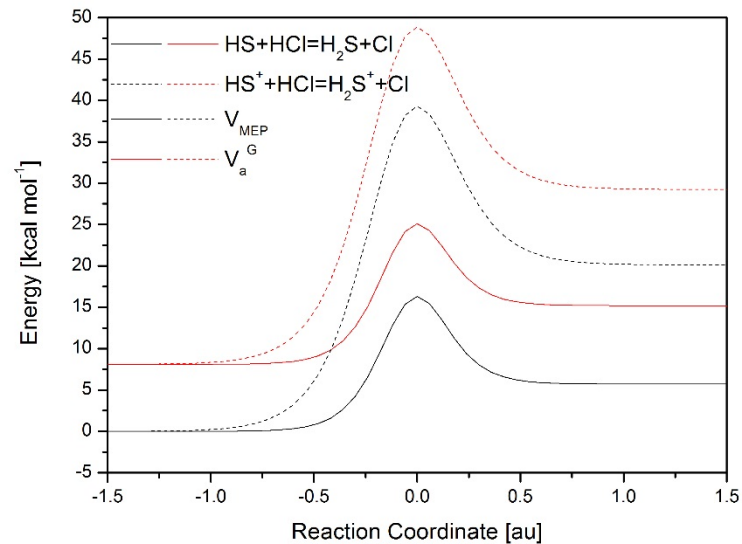
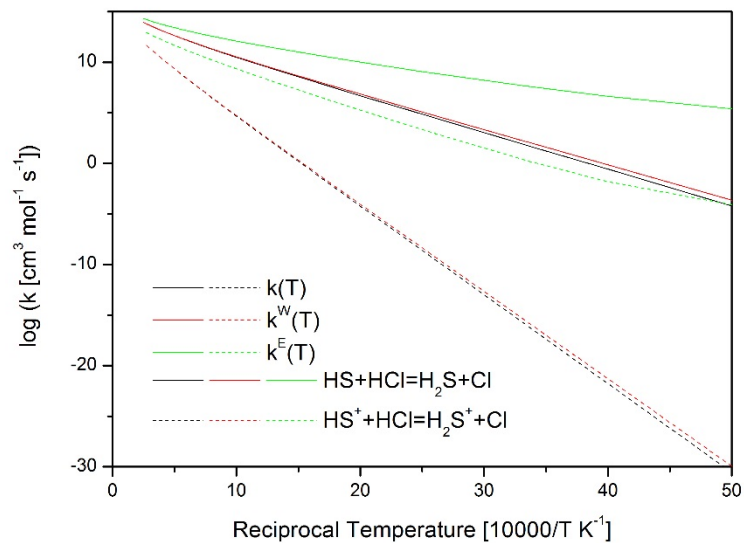
 reagentes.dat

 tsl.dat

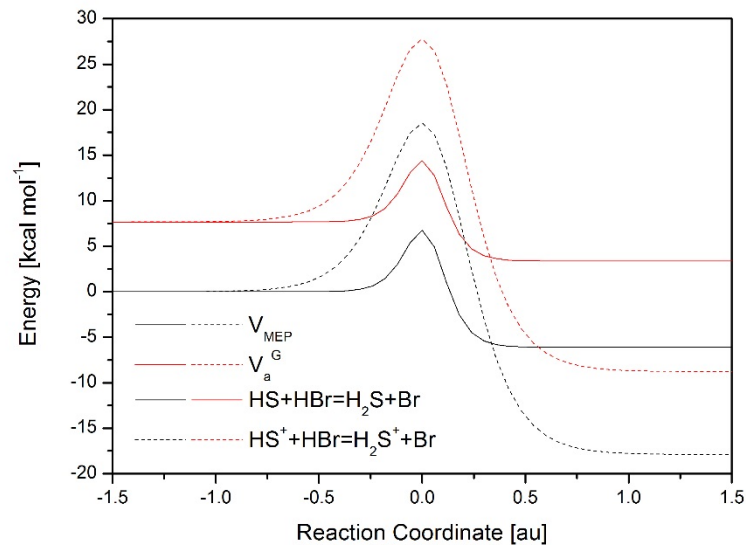
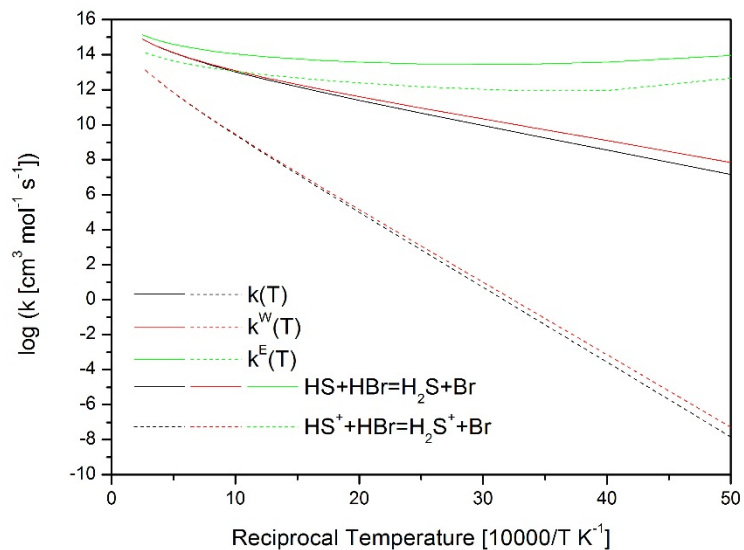




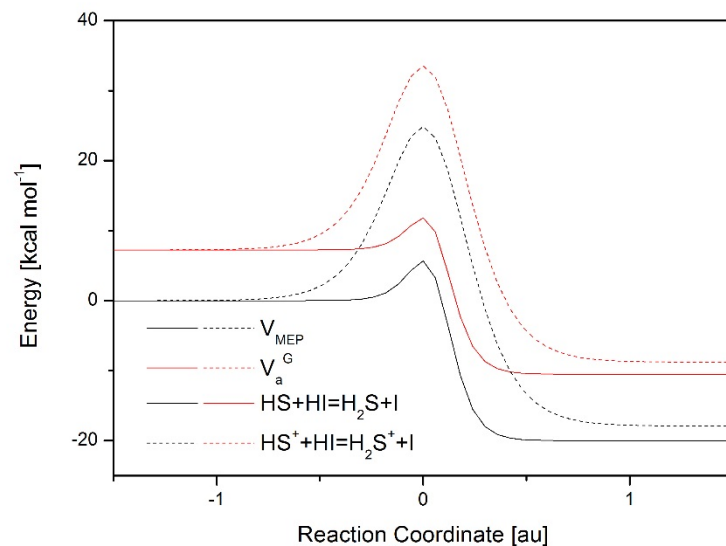
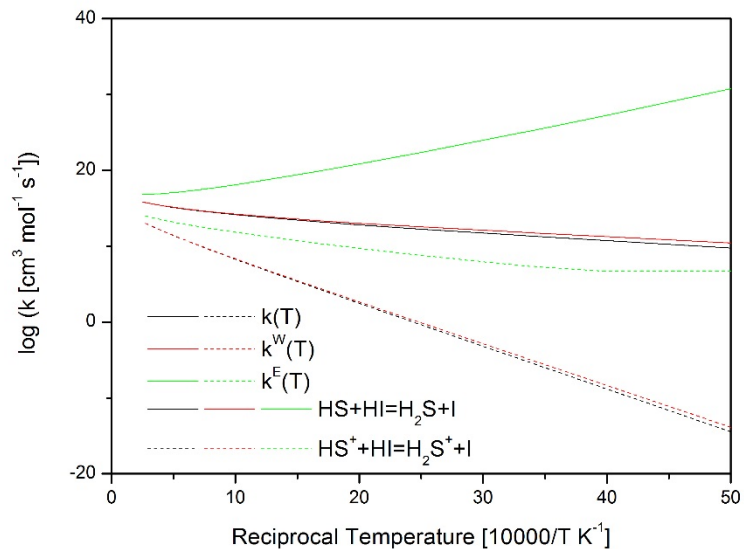
# $HS+HCl=H_2S+Cl$ or $HS^++HCl=H_2S^++Cl$



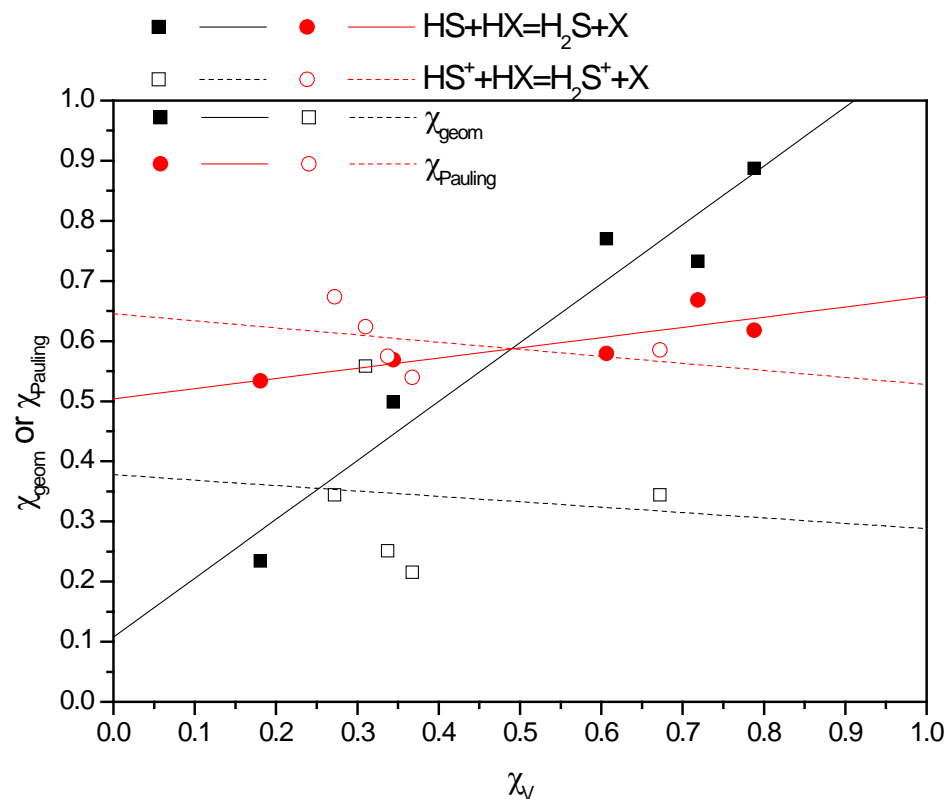
# $HS+HBr=H_2S+Br$ or $HS^++HBr=H_2S^++Br$



# $HS+HI=H_2S+I$ or $HS^++HI=H_2S^++I$



# Hammond's Postulate



$$\chi(V) = \frac{V_f^+}{V_f^+ + V_r^+}$$

$$\chi(\text{geom}) = \frac{(r_1 - r_{1,eq})_b}{(r_1 - r_{1,eq})_b + (r_2 - r_{2,eq})_m}$$

$$\chi(\text{Pauling}) = \frac{n_m}{n_m + n_b}, \quad n = \exp[-\beta(r - r_{eq})]$$



# Arrhneius rate

	Conventional			Wigner			Eckart		
TS	A	n	Ea	A	n	Ea	A	n	Ea
HS-H <sub>2</sub>	6.16E+08	1.61	14473.00	2.22E+08	1.72	13474.00	3.85E+05	2.47	1143.00
HS-HF	3.71E+09	1.17	43691.00	1.25E+09	1.29	42976.00	4.59E+06	1.95	9343.60
HS-HCl	3.11E+09	1.47	15548.00	1.06E+09	1.59	14847.00	1.86E+07	2.07	6354.20
HS-HBr	2.06E+09	1.63	5342.90	6.71E+08	1.75	4512.10	7.49E+06	2.28	-1408.60
HS-HI	3.01E+09	1.82	3589.20	9.83E+08	1.95	2771.40	4.59E+07	2.31	-16085.00
HS-H <sub>2</sub> <sup>+</sup>	1.11E+10	0.89	27110.00	3.63E+09	1.01	26291.00	7.58E+02	2.83	-16214.00
HS-HF <sup>+</sup>	3.71E+09	1.17	24460.00	1.25E+09	1.29	23745.00	2.07E+05	2.32	-9770.10
HS-HCl <sup>+</sup>	1.48E+09	1.35	39102.00	4.88E+08	1.48	38347.00	8.31E+04	2.50	14353.00
HS-HBr <sup>+</sup>	2.37E+09	1.36	18528.00	8.14E+08	1.48	17842.00	1.74E+06	2.21	-635.64
HS-HI <sup>+</sup>	3.30E+09	1.40	24825.00	1.10E+09	1.52	24085.00	7.07E+04	2.66	4929.70

	A	n	Ea	Ref	Ti	Tf
<b>SH + HBr = Br + H2S</b>	<b>2.65E+12</b>		<b>971.00</b>	<b>92NIC/KRE</b>	<b>299.00</b>	<b>423.00</b>
Br + H2S = HBr + SH	8.43E+12		2750.00	97DEM/SAN	200.00	300.00
	8.55E+12		2752.00	92NIC/KRE	319.00	431.00
F + H2S = HF + SH	7.71E+13			87SCH/RAH	298.00	00
Cl + H2S = HCl + SH	2.23E+13		-210	97DEM/SAN	200	300
	2.23E+13		-208	97ATK/BAU2	200	430
	2.22E+13		-208	95NIC/WAN	202	430
	6.32E+13			86LU/IYE	232	359
	3.78E+13			85NAV/BRO	211	353
	3.07E+13			84CLY/MAC	296	
	2.41E+13			83CLY/ONO	298	
	4.40E+13			80NES/LEO	298	
	3.61E+13			78BRA/LEO	296	
H + H2S = H2 + SH	1.18E+07	2.1	352	92YOS/KOS	293	2237
	4.46E+11			83CLY/ONO	298	8
	1.08E+13		1500	82ROT/LOH	1965	2560
	5.18E+11			80HUS/SLA	300	
	4.82E+11			79WOJ/BAJ	298	
	5.00E+11			79NIC/AMO	295	
	2.75E+13		330	77PRA/ROG	808	937
	9.04E+12		855	73SCH2	190	500
	5.00E+11			73BRA/TRU	298	298
	2.29E+11			72ROM/SCH	298	
	7.76E+12		860	71KUR/PET	190	464
	1.02E+13		845	70MIH/SCH	243	368
	1.93E+12			70CUP/GLA	295	
	7.69E+11			69PER/FRA	298	

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Thank you

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